

Some Useful Maple Commands

d i f f: Compute symbolic derivatives

$$\left[\begin{array}{l} > \text{ex1} := \exp(\sin(4*x)) + \ln(x^2 + \sqrt{x}); \\ \text{ex1} := e^{\sin(4x)} + \ln(x^2 + \sqrt{x}) \end{array} \right]$$

$$\left[\begin{array}{l} > \text{diff}(\text{ex1}, x); \\ 4 \cos(4x) e^{\sin(4x)} + \frac{2x + \frac{1}{2\sqrt{x}}}{x^2 + \sqrt{x}} \end{array} \right]$$

Higher order derivatives

$$\left[\begin{array}{l} > \text{diff}(\text{ex1}, x, x); \\ -16 \sin(4x) e^{\sin(4x)} + 16 \cos(4x)^2 e^{\sin(4x)} + \frac{2 - \frac{1}{4x^{3/2}}}{x^2 + \sqrt{x}} - \frac{\left(2x + \frac{1}{2\sqrt{x}}\right)^2}{(x^2 + \sqrt{x})^2} \end{array} \right]$$

equivalently ...

$$\left[\begin{array}{l} > \text{diff}(\text{ex1}, x\$2); \\ -16 \sin(4x) e^{\sin(4x)} + 16 \cos(4x)^2 e^{\sin(4x)} + \frac{2 - \frac{1}{4x^{3/2}}}{x^2 + \sqrt{x}} - \frac{\left(2x + \frac{1}{2\sqrt{x}}\right)^2}{(x^2 + \sqrt{x})^2} \end{array} \right]$$

Multivariate differentiation

Note nesting of **d i f f** commands

$$\left[\begin{array}{l} > \text{diff}(\text{diff}(\cos(x/y), x), y); \\ \frac{\cos\left(\frac{x}{y}\right)x}{y^3} + \frac{\sin\left(\frac{x}{y}\right)}{y^2} \end{array} \right]$$

i n t: Compute symbolic integrals (anti-derivatives and definite integrals)

$$\left[\begin{array}{l} > \text{ex2} := 1 / \text{sqrt}(x^2 - a^2); \\ \text{ex2} := \frac{1}{\sqrt{-a^2 + x^2}} \end{array} \right]$$

```
[ > int( ex2 , x );
```

$$\ln(x + \sqrt{-a^2 + x^2})$$

Observe that the output does not include an arbitrary constant of integration

Definite integrals

```
[ > int( x^2 , x = 0 .. 2 );
```

$$\frac{8}{3}$$

Don't expect miracles!! I.e. many expressions have no definite integral expressible in terms of elementary functions. in which case the output from Maple is identical to the input

```
[ > int( ex1, x );
```

$$\int (e^{\sin(4x)} + \ln(x^2 + \sqrt{x})) dx$$

Multi-dimensional integrals are often straightforward ... note nesting of `int` commands

```
[ > ex3 := (x^3 + y^3) / (x^2 - y^2);
```

$$ex3 := \frac{x^3 + y^3}{x^2 - y^2}$$

```
[ > int( int(ex3, x), y );
```

$$\frac{1}{6} x^2 y - \frac{1}{3} (x-y)^3 \ln(x-y) - \frac{1}{9} y^3 - \frac{1}{6} y^2 x + \frac{11}{18} x^3 + x y^2 \ln(x-y) - \ln(x-y) y x^2$$

series and taylor: Compute power series expansions

```
[ > series( exp(x) , x = 0 );
```

$$1 + x + \frac{1}{2} x^2 + \frac{1}{6} x^3 + \frac{1}{24} x^4 + \frac{1}{120} x^5 + O(x^6)$$

Optional third argument specifies expansion order

```
[ > series( exp(x), x = 0, 11);
```

$$1 + x + \frac{1}{2} x^2 + \frac{1}{6} x^3 + \frac{1}{24} x^4 + \frac{1}{120} x^5 + \frac{1}{720} x^6 + \frac{1}{5040} x^7 + \frac{1}{40320} x^8 + \frac{1}{362880} x^9 + \frac{1}{3628800} x^{10} + O(x^{11})$$

For purposes of course, **taylor** and **series** are synonymous commands

```
[ > taylor( exp(x), x = 0);  
      1 + x +  $\frac{1}{2} x^2 + \frac{1}{6} x^3 + \frac{1}{24} x^4 + \frac{1}{120} x^5 + O(x^6)$ 
```

The special Maple variable **Order** controls the default expansion order

```
[ > Order := 8;  
      Order:= 8
```

```
[ > taylor(exp(x), x = 0);  
      1 + x +  $\frac{1}{2} x^2 + \frac{1}{6} x^3 + \frac{1}{24} x^4 + \frac{1}{120} x^5 + \frac{1}{720} x^6 + \frac{1}{5040} x^7 + O(x^8)$ 
```

```
[ > Order := 6;  
      Order:= 6
```

```
[ > taylor_exp := taylor(exp(x), x = 0);  
      taylor_exp:= 1 + x +  $\frac{1}{2} x^2 + \frac{1}{6} x^3 + \frac{1}{24} x^4 + \frac{1}{120} x^5 + O(x^6)$ 
```

Convert the last Taylor series to a polynomial (useful for Homework 2!)

```
[ > taylor_exp_p := convert(taylor_exp, polynomial);  
      taylor_exp_p:= 1 + x +  $\frac{1}{2} x^2 + \frac{1}{6} x^3 + \frac{1}{24} x^4 + \frac{1}{120} x^5$ 
```

Evaluate the series approximation (polynomial) for $x = 0.2$

```
[ > res1 := evalf( subs(x = 0.2, taylor_exp_p) );  
      res1:= 1.221402667
```

Compute the corresponding exact value as a floating point number

```
[ > res2 := exp(0.2);  
      res2:= 1.221402758
```

Compute the error in the approximation

```
[ > err := res1 - res2;
```

```
[ err:= -9.1 10-8
```

solve: Solve equations, including linear systems

```
[ > eq1 := x + y + z = 6; eq2 := 2 * x + y + z = 2;  
  eq3 := x + y + 3 * z = 3;  
  eq1:= x + y + z = 6  
  eq2:= 2 x + y + z = 2  
  eq3:= x + y + 3 z = 3
```

```
[ > solve( {eq1, eq2, eq3} , {x, y, z} );  
  {x = -4, y =  $\frac{23}{2}$ , z =  $-\frac{3}{2}$ }
```

Since there are only three distinct names in the set of equations, Maple can deduce that they are the three unknowns ...

```
[ > solve( {eq1, eq2, eq3} );  
  {x = -4, y =  $\frac{23}{2}$ , z =  $-\frac{3}{2}$ }
```

Common mistakes

(1) Not terminating statement with ';' or ':'

```
[ > a := int(x^2, x = 0..1)  
  Warning, inserted missing semicolon at end of statement  
  a:=  $\frac{1}{3}$ 
```

(2) Using '=' rather than ':=' for assignment ... the following evaluates as an equation (whose logical value is false)

```
[ > a = 2;  
   $\frac{1}{3} = 2$ 
```

The variable **a** was previously assigned a value, which was not altered by the above statement

```
[ > a;  
   $\frac{1}{3}$ 
```

This is what we meant to type

```
[ > a := 2;
                                     a:= 2
```

```
[ > a;
                                     2
```

(3) Using single quotes (') rather than double quotes (") to delimit strings

```
[ > string1 := "This is a Maple string";
                                     string1 := "This is a Maple string"
```

```
[ > string2 := 'This is not a Maple string';
Error, missing operator or `:`
```